
Edge -Balance Index Sets of Helm

J. Jeba Jesintha¹, V. Sharon Philomena¹, K.Thirusangu², B. Pavithra¹

¹ Department of Mathematics Women's Christian College, Chennai

² Department of Mathematics S.I.V.E.T. College

E-mail: jjesintha_75@yahoo.com

Abstract

The edge-balance index set of a graph $G(V, E)$ was defined by Chopra, Lee and Su[1] in 2010 as follows: For an edge labeling $f: E(G) \rightarrow \{0, 1\}$, a partial vertex labeling $f^*: V(G) \rightarrow \{0, 1\}$ is defined as

$$f^*(v) = \begin{cases} 0, & \text{if more edges with label 0 are incident to } v \\ 1, & \text{if more edges with label 1 are incident to } v \\ \text{unlabeled,} & \text{otherwise} \end{cases}$$

For $i = 0$ or 1 , let $A = \{uv \in E : f(uv) = i\}$ and $B = \{v \in V : f^*(v) = i\}$

Let $e_G(i) = |A|$ and $v_G(i) = |B|$. The edge balance index set of G denoted as $EBI(G)$ is computed as $EBI(G) = \{ |v_G(0) - v_G(1)| : \text{the edge labeling } f \text{ satisfies } |e_G(0) - e_G(1)| \leq 1 \}$. The edge-balance index set for the fan graph F_{n-1} where $F_{n-1} = P_{n-1} + K_1$ and wheel graph W_n , where $W_n = C_{n-1} + K_1$ was obtained by Lee, Tao, Lo[5]. In this paper, we compute the edge-balance index set for the Helm graph, where the Helm graph is defined as the graph obtained from a wheel graph by attaching a pendant edge at each vertex of the n - cycle.
