

# Symptoms of Breast Cancer – An Analysis Using Induced Fuzzy Cognitive Maps (IFCMS)

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**Abstract** - Cancer is a disease in which cells become abnormal and form more cells in an uncontrolled way. With breast cancer, the cancer begins in the tissues that make up the breasts. The cancer cells may form a mass called a tumor. (Note: Not all tumors are cancer.) They may also invade nearby tissue and spread to lymph nodes and other parts of the body. The most common types of breast cancer are: Ductal carcinoma – Cancer that begins in the ducts and grows into surrounding tissues. About 8 in 10 breast cancers are this type. Lobular carcinoma (LAH-byuh-luhr KAR-sih-NOH-muh) – Cancer that begins in lobules and grows into surrounding tissues. About 1 in 10 breast cancers are this type. Hence, this research investigates the most contributing /impactful factor of symptoms of breast cancer using Induced Fuzzy Cognitive Maps (IFCMs). IFCMs are a fuzzy-graph modeling approach based on expert's opinion. This is the non-statistical approach to study the problems with imprecise information. In the current study, Section 1 introduction about cancer. Section 2 overviews the Fuzzy Cognitive Map theory, and its influence. Section 3 explains the Algorithmic approach of IFCM models. Section 4 discusses the components (attributes) symptoms of breast cancer and implementation of IFCM model and Section 5 reveals the conclusion of the problem.

**Keywords**- Breast cancer, IFCM, Symptoms.

## I. INTRODUCTION

Cancer is the general name for a group of more than 100 diseases. Although there are many kinds of cancer, all cancers start because abnormal cells grow out of control. The body is made up of trillions of living cells. Normal body cells grow, divide, and die in an orderly fashion. During the early years of a person's life, normal cells divide faster to allow the person to grow. After the person becomes an adult, most cells divide only to replace worn-out or dying cells or to repair injuries[1].

By Dr Ananya Mandal, MD says that "Cancer possess the same common properties of:

- abnormal cell growth
- capacity to invade other tissues
- capacity to spread to distant organs via blood vessels or lymphatic channels (metastasis)

Untreated cancers can cause serious illness by invading healthy tissues and lead to death"[2]. Fuzzy Cognitive Maps (FCMs) is a well established technique for prediction and decision making especially for situations where fuzziness and uncertainty exists. To deal imprecise information, Lofti A. Zadeh, 1965, introduced the notion of fuzziness. In 1986, Kosko[3], the guru of fuzzy logic introduced the Fuzzy-

Cognitive Maps. It was a fuzzy extension of the Cognitive Map pioneered in 1976 by Political Scientist Robert Axelrod, who used it to represent knowledge as an interconnected, directed, bi-level logic graph. Thus the FCM plays a vital role in modeling system. This paper describes the method of analyzing the most contributing factor symptoms of breast cancer using Induced Fuzzy Cognitive Maps (IFCMs) which was introduced by T. Pathinathan[13] and which is the advanced study of FCM[4,5]. It is worth mentioning here, the book entitled 'FCMs and Neutrosophic Cognitive Maps' by Vasantha and Smarandache, 2003[6]. This book infers that FCMs strongly resemble neural networks and powerful for reaching consequences as a mathematical tool for modeling complex systems. Implications for interdisciplinary reading: National Implication by Calais[7], FCM based tool for prediction of infectious diseases by Elpiniki et al., [7], Benefit of literacy in Bhutan by Devadoss et al., [8], Problem faced by bonded labourers near Kodaikanal forests discussed and solution given by Vasantha[9] are notable studies in this area of research. In all the above studies, the various real life with imprecise information taken and the precise solutions given by FCM and its advanced studies.

## II. FUZZY COGNITIVE MAPS

Fuzzy Cognitive Maps (FCMs) are digraphs that capture the cause/effect relationship in a system. Nodes of the graph stand for the concepts representing the key factors and attributes of the modeling system, such as inputs, variable states, components factors, events, actions of any system. Signed weighted arcs describe the causal relationships, which exist among concepts and interconnect them, with a degree of causality. The constructed graph clearly shows how concepts influence each other and how much the degree of influence is. Cognitive Maps (CMs) were proposed for decision making by Axelrod[10] for the first time. Using two basic types of elements; concepts and causal relationship, the cognitive map can be viewed as a simplified mathematical model of a belief system. FCMs were proposed with the extension of the fuzzified causal relationships. Kosko[3], introduced FCMs as a fuzzy graph structures for representing causal reasoning. When the nodes of the FCM are fuzzy sets then they are called fuzzy nodes. FCMs with edge weights or causalities from the set  $\{-1, 0, 1\}$  are called simple FCMs. Consider the nodes/concepts  $P_1, P_2, P_3, \dots, P_n$  of the FCM. Suppose the directed graph is drawn using edge weights  $e_{ij}$  from  $\{-1, 0, 1\}$ . The matrix  $M$  defined by  $M = (e_{ij})$  where  $e_{ij}$  is the weight of the directed edge  $P_i P_j$ .  $M$  is called the adjacency matrix of the FCM, also known as connection matrix. The directed edge  $e_{ij}$  from the causal concept  $P_i$  to concept  $P_j$  measures how much  $P_i$  causes  $P_j$ . The edge  $e_{ij}$  takes values in the real interval  $[-1, 1]$ .

$e_{ij}=0$  indicates no causality.

$e_{ij}>0$  indicates causal increase/Positive causality.

$e_{ij}<0$  indicates causal decrease/Negative causality.

Simple FCMs provide quick first-hand information to an expert's stated causal knowledge. Let  $P_1, P_2, P_3, \dots, P_n$  be the nodes of FCM. Let  $A=(a_1, a_2, \dots, a_n)$  is called a state vector where either  $a_i=0$  or  $1$ . If  $a_i=0$ , the concept  $a_i$  is in the OFF state and if  $a_i=1$ , the concept  $a_i$  is in the ON state, for  $i=1, 2, \dots, n$ . Let  $P_1, P_2, P_3, \dots, P_i, P_j, \dots$  be the edges of the FCM ( $i \neq j$ ). Then the edges form a directed cycle.

### III. AN FCM IS SAID TO BE CYCLIC IF IT POSSESSES A DIRECTED CYCLE

An FCM with cycles is said to have a feedback, when there is a feedback in an FCM, i.e., when the causal relations flow through a cycle in a revolutionary way, the FCM is called a dynamical system. The equilibrium state for the dynamical system is called the hidden pattern. If the equilibrium state of a dynamical system is a unique state vector, it is called a fixed point or limit cycle. Inference from the hidden pattern summarizes the joint effect of all interacting fuzzy knowledge.

#### A. Algorithmic approach in IFCM

Even though IFCM is an advancement of FCM it follows the foundation of FCM, it has a slight modification only in Algorithmic approaches. To derive an optimistic solution to the problem with an unsupervised data, the following steps to be followed:

- Step 1: For the given model (problem), collect the unsupervised data that is indeterminate factors called nodes.
- Step 2: According to the expert opinion, draw the directed graph.
- Step 3: Obtain the connection matrix,  $M_1$ , from the directed graph (FCM). Here the number of rows in the given matrix = number of steps to be performed.
- Step 4: Consider the state vector  $S(X_1)$  by setting  $c_1$  in ON position that is assigning the first component of the vector to be 1 and the rest of the components as 0. Find  $S(X_1) \times M_1$ . The state vector is updated and threshold at each stage.
- Step 5: Threshold value is calculated by assigning 1 for the values  $>0$  and 0 for the values  $<1$ . The symbol ' $\hookrightarrow$ ' represents the threshold value for the product of the result.
- Step 6: Now each component in the  $C_1$  vector is taken separately and product of the given matrix is calculated. The vector which has maximum number of one's is found. The vector with maximum number of one's which occurs first is considered as  $C_2$ .
- Step 7: When the same threshold value occurs twice. The value is considered as the fixed point. The iteration gets terminated.
- Step 8: Consider the state vector  $C_1$  by setting  $C_2$  in ON state that is assigning the second component of the vector to be 1 and the rest of the components as 0. Proceed the calculations discussed in Steps 4 to 6.
- Step 9: Continue Step 9 for all the state vectors and find hidden pattern.

### IV. ABOUT BREAST CANCER

Breast cancer is a disease in which certain cells in the breast become abnormal and multiply without control or order to form a tumor. The most common form of breast cancer begins in cells lining the ducts that carry milk to the nipple (ductal cancer). Other forms of breast cancer begin in the glands that produce milk (lobular cancer) or in other parts of the breast. Early breast cancer usually does not cause pain and may exhibit no noticeable symptoms. As the cancer progresses, signs and symptoms can include a lump or thickening in or near the breast; a change in the size or shape of the breast; nipple discharge, tenderness, or retraction (turning inward); and skin irritation, dimpling, or scaliness. These changes can occur as part of many different conditions, however. Having one or more of these symptoms does not mean that a person definitely has breast cancer. In some cases, cancerous tumors can invade surrounding tissue and spread to other parts of the body. If breast cancer spreads, cancerous cells most often appear in the bones, liver, lungs, or brain. Tumors that begin at one site and then spread to other areas of the body are called metastatic cancers. A small percentage of all breast cancers cluster in families. Hereditary cancers are those associated with inherited gene mutations. Hereditary breast cancers tend to occur earlier in life than non inherited (sporadic) cases and are more likely to involve both breasts.

Researchers estimate that more than 178,000 new cases of invasive breast cancer will be diagnosed in U.S. women in 2007. Most breast cancers occur in women, but they can also develop in men. Scientists estimate that more than 2,000 new cases of breast cancer will be diagnosed in men in 2007. An estimated 5 percent to 10 percent of all breast cancers are hereditary. Particular mutations in genes associated with breast cancer are more common among certain geographic or ethnic groups, such as people of Ashkenazi (central or eastern European) Jewish heritage and people of Norwegian, Icelandic, or Dutch ancestry. Particular genetic changes occur more frequently in these groups because they have a shared ancestry over many generations [11]. The crude breast cancer cases in urban Indian women is 25-30 and the age adjusted rate is 30-35 new cases per 1,00,000 women per year. Breast cancer is increasing – the average increase over a 30 year period in Mumbai was 11 per cent per decade. Breast cancer is increasing both in young (11 per cent per decade) and old women (16 per cent per decade). There are an estimated 1,00,000-1,25,000 new breast cancer cases in India every year. The number of breast cancer cases in India is estimated to double by 2025 [12].

#### A. Symptoms of Breast Cancer

In its early stages, breast cancer usually has no symptoms. As a tumor develops, you may note the following signs: A lump in the breast or underarm that persists after your menstrual cycle. This is often the first apparent symptom of breast cancer. Lumps associated with breast cancer are usually painless, although some may cause a prickly sensation. Lumps are usually visible on a mammogram long before they can be seen or felt.

- Swelling in the armpit.

- Pain or tenderness in the breast. Although lumps are usually painless, pain or tenderness can be a sign of breast cancer.
- A noticeable flattening or indentation on the breast, which may indicate a tumor that cannot be seen or felt.
- A marble-like area under the skin.
- Any change in the size, contour, texture, or temperature of the breast. A reddish, pitted surface like the skin of an orange could be a sign of advanced breast cancer.
- A change in the nipple, such as a nipple retraction, dimpling, itching, a burning sensation, or ulceration. A scaly rash of the nipple is symptomatic of Paget's disease, which may be associated with an underlying breast cancer.
- Unusual discharge from the nipple that may be clear, bloody, or another color. It's usually caused by benign conditions but could be due to cancer in some cases.
- An area that is distinctly different from any other area on either breast.

#### B. Adaptation of IFCM to the problem

To analyze the symptoms of breast cancer, we have interviewed and discussed with 100 women in different ages from 26 to 65 in adyar cancer institute and with the experts opinion we have taken the following attributes.

$c_1$  - swelling of all or part of the breast

$c_2$  - skin irritation or dimpling

$c_3$  - breast pain

$c_4$  - nipple pain or the nipple turning inward

$c_5$  - redness, scaliness, or thickening of the nipple or breast skin

$c_6$  - a nipple discharge other than breast milk

$c_7$  - a lump in the underarm area

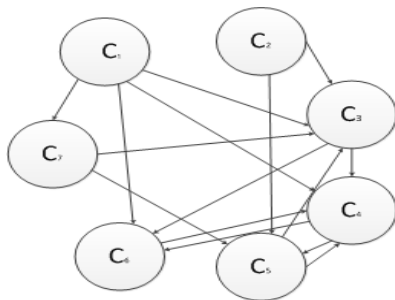


Figure-1

Figure-1 gives the directed graph with  $c_1, c_2, \dots, c_7$  as nodes

The connection matrix  $M_1$  related to the graph in Figure-1. is given below.

$$M_1 = \begin{pmatrix} 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 \end{pmatrix}$$

Step 1-Let us consider  $S(X_1)$  in the step1, by setting the concept  $c_1$  to ON state i.e., the first component of the vector is set to be 1 and the rest are assigned to 0.

$$S(X_1) = (1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)$$

$$S(X_1)M_1 = (0 \ 0 \ 1 \ 1 \ 0 \ 1 \ 1) \\ \hookrightarrow (0 \ 0 \ 1 \ 1 \ 0 \ 1 \ 1) = C_0'$$

$$C_0' M_1 \approx$$

$$(0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0)M_1 = (0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0) \\ = C_1.$$

$$(0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0)M_1 = (0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0)$$

$$(0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0)M_1 = (0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0)$$

$$(0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1)M_1 = (0 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0)$$

$$C_1 M_1 = (0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 0) \hookrightarrow (0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 0)$$

$$(0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0)M_1 = (0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0) \\ = C_2$$

$$(0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0)M_1 = (0 \ 0 \ 1 \ 1 \ 0 \ 0 \ 0)$$

$$(0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0)M_1 = (0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0)$$

$$C_2 M_1 = (0 \ 0 \ 1 \ 2 \ 0 \ 0 \ 0) \hookrightarrow \\ (0 \ 0 \ 1 \ 1 \ 0 \ 0 \ 0)$$

$$(0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0)M_1 = (0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0) \\ = C_3 = C_1.$$

$$(0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0)M_1 = (0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0)$$

The fixed point is  $(0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0)$  When the same threshold value occurs twice, the value is considered as the fixed point. The iteration gets terminated and the calculation gets terminated. When the first attribute is kept in ON state, we get the triggering pattern as  $C_1 \Rightarrow C_3 \Rightarrow C_4 \Rightarrow C_3$ . Similarly, we get the following table, which gives the triggering pattern for each step.

Table:1

Stepno	AttributeON	Triggering pattern
Step 1	$c_1$	$c_1 \Rightarrow c_3 \Rightarrow c_4 \Rightarrow c_3$
Step 2	$c_2$	$c_2 \Rightarrow c_3 \Rightarrow c_4 \Rightarrow c_3$
Step 3	$c_3$	$c_3 \Rightarrow c_4 \Rightarrow c_3$
Step 4	$c_4$	$c_4 \Rightarrow c_5 \Rightarrow c_4$
Step 5	$c_5$	$c_5 \Rightarrow c_3 \Rightarrow c_4 \Rightarrow c_3$
Step 6	$c_6$	$c_6 \Rightarrow c_4 \Rightarrow c_3 \Rightarrow c_4$
Step 7	$c_7$	$c_7 \Rightarrow c_3 \Rightarrow c_4 \Rightarrow c_3$

Merging all these induced paths on a singlegraph we obtain the following Graph.

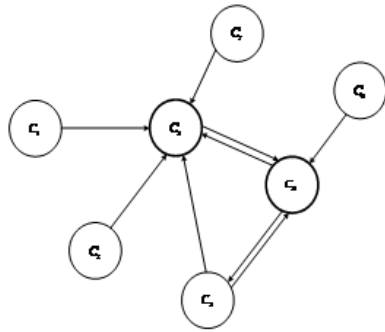


Figure-2  
**V.CONCLUSION**

From the above calculation, breast pain and nipple pain or the nipple turning inward is the main symptom to alert one to the medical verification of breast cancer. We have observed that when any one of the symptoms of breast cancer (attributes) is switched onto ON state,  $c_3$  and  $c_4$  goes to ON state. The Induced FCM method clearly highlights the interrelationship with all the other attributes to the symptom of breast pain and nipple pain or the nipple turning inward pain in breast.

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